

Answer Key: Calculating Efficiency

Step 1: We start by recalling the formula for chemical efficiency, which is equal to the kinetic energy of the expelled exhaust over the potential energy contained within the fuel: $\frac{1}{2} * m * v^2 / m q$.

Step 2: Next, since we assume that the mass of the original fuel is the same as the mass of the exhaust, we can cancel out the masses, leaving us with the formula $\text{efficiency} = v^2 / 2q$

Step 3: Now we can just plug in our numbers: $\text{efficiency} = (600)(600)/(2)(5*10^6) = .035 = 3.5\%$

For those interested, this is a little bit higher than the true measured efficiency of Goddard's early rockets of around 2%. This is likely due to the assumption we made: in reality, the mass of the exhaust ejected will be smaller than the mass of the fuel, as debris from combustion will be left within the combustion chamber and nozzle,